

Winds of change in math education

Prof. Zbigniew Marciniak Faculty of Mathematics, Informatics and Mechanics, University of Warsaw











Surveyor at Stanford U.

Me: "How do you use ArcSecant ?"

Him: "I don't – it's computerized"





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The New York Times

Trump's Lies

Many Americans have become accustomed to President Trump's lies. But as regular as they have become, the country should not allow itself to become numb to them. So we have catalogued nearly every outright lie he has told publicly since taking the oath of office. Updated: The president is still lying, so we've added to this list, taking it through Nov. 11, and provided links to the facts in each case.

JAN. 21 "I wasn't a fan of Iraq. I didn't want to go into Iraq." (*He was for an invasion before he was against it.*) JAN. 21 "A reporter for Time magazine — and I have been on their cover 14 or 15 times. I think we have the all-time record in the history of Time magazine." (*Trump was on the cover 11 times and Nixon appeared 55 times.*) JAN. 23 "Between 3 million and 5 million illegal votes caused me to lose the popular vote." (*There's no evidence of illegal voting.*) JAN. 25 "Now, the audience was the biggest ever. But this crowd was massive. Look how far back it goes. This crowd was massive." (*Official aerial photos show Obama's 2009 inauguration was much more heavily attended.*) JAN. 25 "Take a look at the Pew reports (which show voter fraud.)" (*The report never mentioned voter fraud.*) JAN. 25 "You had millions of people that now aren't insured anymore." (*The real number is less than 1 million, according to the Urban Institute.*) JAN. 25 "So, look, when President Obama was there two weeks ago making a speech, very nice speech. Two people were shot and killed during his speech. You can't have that." (*There were no gun homicide victims in Chicago*)

SECTIONS C HOME Q SEARCH

Winds of change... The Age of Post-Truth Politics

The New York Times

President Trump's lies. country should not allow e catalogued nearly every the oath of office. Updated: to this list, taking it through h each case.

Lies

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People demonstrated in London against Brexit in July. Andrew Testa for The New York Times

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By WILLIAM DAVIES AUG. 24, 2016

SECTIONS



Conclusions for education

Prepare students to be ready to deal also with non-routine tasks

Prepare students to recognize and deal with lies

How to achieve that?



Why do we have to learn mathematics?!

Practice patiently – you will see why later!



Practice patiently – you will see why this makes sense later!





Mr. Jones, will I ever use this algebra?You won't, but some smarter kids might!

Why do I have to learn percentages? ... fractions? ... logarithms?

.... f

Concept orinted teaching



Concept orinted teaching



Why do I have to learn percentages? ... fractions? ... logarithms?













* AGENDA * MATHEMATICS FOR THE 21st CENTURY

Friday May 25, 2018

-	Hosted by the International School of Geneva,
	Route de Chêne 62, Centre des Arts, Genève, Switzerland
8:30 - 9:00	Coffee/tea and light pastries
9:00 - 9:30	Introductions, welcome, setting the stage
	 Greetings and introduction: Fondation IIelvetica Educatio, International School of Geneva, Jacobs Foundation, Gebert Ruf Foundation, Wright Foundation (10 mins)
	 Greetings, remarks on importance to OECD countries (10 mins): Andreas Schleicher (OECD).
	• TBD Swiss Federal representative for Mathematics (5 mins).
	Greetings: Urs Lang (Swiss Mathematical Society) (5 mins).
9:30 - 10:00	Presentation: <i>Mathematics for the modern world</i> – Charles Fadel (Center for Curriculum Redesign)
10:00 10:45	Presentation: <i>Recommendations for PISA</i> Michelle Bruniges (Australia; Chair of PISA Governing Board) including 15 minutes for Q&A
Break 15 minutes	Coffee/tea and light pastries
11:00 11:45	Presentation: How Poland moved ahead - Zbigniew Marciniak (Warsaw University) including 15 minutes for Q&A
11:45 - 12:45	Presentation: Stop Teaching Calculating, Start Teaching Maths – Conrad Wolfram (Wolfram Research) including 15 minutes for Q&A
Lunch @ 12:45 pm	In cafeteria on-site at EcolInt/ISG
13:45 - 14:45	Presentation: Mathematics and the Brain – Stanislas Deheane (CNRS) including 15 minutes for Q&A
Break 15 minutes	Coffee/tea
15:00 - 16:00	Presentation: What Mathematics do people really need? Keith Devlin (Stanford University) including 15 minutes for Q&A
16:00 -17:00	Presentation: Algorithms do change the world! – John MacCormick (Dickinson College) including 15 minutes for Q&A
17:00 – 17:30 then adjourn	Final remarks and Instant Poll: What do we de-emphasize and remove? Charles Fadel (Center for Curriculum Redesien) and wishes for success.



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© Charles Fadel Occupation (below)	Algebra	Applied Maths	Calculus	Discrete Mathematics	Foundations	Geometry	Numbers & Operations	Statistics & Probability	Topology & Recreational
Taxonomy & Ontology: Wolfram Research →	Matrices, Operations, Vectors etc	Complex systems, Control, Game theory, etc	Analysis, Transforms, Polynomials, etc	Automata, Graphs, Computational maths etc	Sets, Logic etc	Curves, Dimensions, Transformations, Trigonometry, etc	Arithmetic operations, Fractions, Sequences, etc	Distributions, Analysis, Estimation, etc	Knots, Figures, Folding, Spaces, etc
Agriculture						Х	X	X	
Architecture		X				X	X	x	х
Astronomy/Cosmology	X	x	x	x		x	X	x	х
Biology, Botany, Zoology		Х		х			X	x	
Biotechnology, Genetics	X	х	X	х		х	X	x	х
Business		x					X	X	
Cinematography/Photography						х	X		х
Civil engineering	х	X	X	X		X	X	X	х
Communication		X					X	x	
Computer science	Х	X	x	X	X	X	X	X	х
Craftsmanship						х	X		х
Dance						X	X		х
Design						x	X		х
Drawing						x	X		х
Economics & Finance	X	х	X	х		X	X	X	
Education	X	x	X			X	X	x	
Electrical engineering	X	X	X	X		X	X	x	
Environmental science	х	х	X	х		Х	х	X	
Ethics							X		
Geography/Geology	х	Х	Х	х		х	X	X	х
Health							X	X	
History/Archeology	х	X		х			X	X	
Journalism	X	X					X	X	
Languages/Linguistics	х	х		х			X	X	
Law		x					X	X	
Materials Science/Nanotechnology	х	х	X	х		X	X	x	х
Mechanical engineering, Robotics	X	X	X	X		Х	X	X	х
Medicine/Pharmacy/Veterinary		х					X	X	
Music	х						X	x	
Painting						X	X		
Philosophy		х			X		х	х	
Physics	х	x	X	x	x	х	X	x	х
Poetry/Prose							X		
Psychology/Sociology/Anthropology	х	X		х			X	X	
Sculpture						x	X		х
Sewing/Knitting/Tapestry						X	X		х
Spirituality/Religions							X		
Theater/Acting							© Center fo	r Curriculum	Redesign

© Charles Fadel									
Occupation (below)									
	Dootr	v. hvric	onic d	ramatic	Dracarn	oval ch	ort story	ccionco	fiction
Taxonomy & Ontology: Wolfram Basaarch	POetr	y. iyric,	epic, u	amatic	Prose. II	over, sn	ort story,	science	
Taxonomy & Ontology. Woman Research 7									
Agriculture						Х	X	X	
Architecture		х				х	X	X	х
Astronomy/Cosmology	х	х	X	х		х	X	X	х
Biology, Botany, Zoology		х		х			x	x	
Biotechnology, Genetics	X	х	Х	х		х	X	x	х
Business		X					X	X	
Cinematography/Photography						х	X		х
Civil engineering	х	х	х	х		х	X	х	х
Communication		x					X	X	
Computer science	x	x	X	х	х	x	X	x	х
Craftsmanship						x	x		х
Dance						x	X		X
Design						х	X		х
Drawing						x	x		x
Economics & Finance	X	х	х	х		х	X	X	
Education	X	х	X			X	X	X	
Electrical engineering	X	х	X	х		X	X	X	
Environmental science	X	х	X	х		х	x	X	
Ethics							x		
Geography/Geology	X	x	х	х		х	X	X	х
Health							X	X	
History/Archeology	X	X		X			X	x	
Journalism	x	x					X	x	
Languages/Linguistics	x	x		х			X	x	
Law		x					X	x	
Materials Science/Nanotechnology	X	x	X	х		x	x	X	х
Mechanical engineering, Robotics	X	х	X	х		х	X	x	х
Medicine/Pharmacy/Veterinary		х					X	X	
Music	X						X	X	
Painting						X	X		
Philosophy		х			х		х	X	
Physics	X	x	X	x	x	х	X	X	х
Poetry/Prose							X		
Psychology/Sociology/Anthropology	X	X		х			X	X	
Sculpture						х	X		х
Sewing/Knitting/Tapestry						x	X		х
Spirituality/Religions							X		
Theater/Acting							© Center fo	r Curriculum	Redesign

© Charles Fadel Occupation (below) Taxonomy & Ontology: Wolfram Research →	Poetr	ry: lyric <i>,</i>	epic, d	ramatic	Prose: r	iovel, sh	ort story,	science	-fiction	
Agriculture Architecture Astronomy/Cosmology Biology, Botany, Zoology	x	x x	x	x		x x x	X X X X	X X X	x x	
Biotechnology, Genetics Business	x	x x	X	x		x	x	x	x	
с с с		Wha	at liter	rature	do pe	ople re	e ally ne	ed?		
Design						X	x		X	
Economics & Einance	×	Y	Y	Y		Ŷ	Ŷ	Y	^	
Education	Ŷ	Ŷ	X	X		x	Ŷ	Ŷ		
	Ŷ	Ŷ	Ŷ	Y		Ŷ	Ŷ	Ŷ		
Environmental science	Ŷ	x	x	x		x	Ŷ	x		
Ethics	^	^	~	X		^	Ŷ	~		
Eulics Geography/Goology	v	v	v	v		v	Ŷ	v	v	
Health	· ^	~	^	~		~	Ŷ	Ŷ	^	
History/Archaology	v	×		×			~	Ŷ		
History/Archeology		Ŷ		~			~	×		
ooumansm Lennuenee/Linnuietiee	l 🗘	×		v			×	× ×		
	^	×		X			X	X		
Law Matasiala Caisasa Nasatashaa'	v	X	×	Y		×	X	X		
Materials Science/Nanotechnology	- X	X	X	X		X	X	X	X	
Medicine (Bloome evel) (stering m	×	X	X	X		X	X	X	x	
Music	v	~					~	× ×		
Nusic Deinting	^					×	×	~		
Failung Bhilesenhu		×			Y	X	X	v		
Philosophy	v	×	×	Y	X	×	×	X	v	
FILYSICS	^	~	*	*	~	~	~	~	^	
Poetry/Prose		×		Y			X	v		
rsychology/Sociology/Anthropology	×	X		x		×	X	X		
Sculpture						X	X		X	
Sewing/Knitting/Tapestry						X	X		X	
Spirituality/Religions							Center fo	r Curriculum	Pedesian	
Theater/Acting	1						S Contrel 10	Guincululli	incues you	

© Charles Fadel Occupation (below)	Poetr	y: lyric,	epic, d	ramatic Pro	se: novel, sho	ort story,	science	-fiction
Taxonomy & Ontology: Wolfram Research →			1 /		,	,,		
Agriculture	l				x	x	x	
Architecture	I	x			х	х	x	x
Astronomy/Cosmology	х	x	X	х	x	x	X	x
Biology, Botany, Zoology		x		Х		х	x	
Biotechnology, Genetics	Х	х	х	Х	х	х	X	x
Business	-	x				x	X	
C C C C		Who	at liter	rature do	people re	ally ne	ed?	

VV//UL //LL/ULU/ people reury necu:

Design					x	x		х	
Drawing					x	X		х	
Economics & Finance	x	x	x	X	x	X	X		

What do we de-emphasize and remove?

Health							X	х	
History/Archeology	X	X		X			X	X	
Journalism	X	x					X	X	
Languages/Linguistics	X	x		X			X	X	
Law		x					X	X	
Materials Science/Nanotechnology	X	x	X	х		x	х	X	x
Mechanical engineering, Robotics	X	X	X	X		х	X	X	x
Medicine/Pharmacy/Veterinary		х					X	X	
Music	x						x	X	
Painting						х	X		
Philosophy		х			х		х	X	
Physics	X	X	X	X	х	х	x	X	x
Poetry/Prose							x		
Psychology/Sociology/Anthropology	X	X		х			X	X	
Sculpture						х	X		x
Sewing/Knitting/Tapestry						x	X		x
Spirituality/Religions							X		
Theater/Acting							© Center for	r Curriculum	Redesign

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Agriculture						X	X	X	
Architecture		x				X	X	x	х
Astronomy/Cosmology	X	x	X	x		X	x	x	х
Biology, Botany, Zoology		х		х			X	x	
Biotechnology, Genetics	Х	Х	Х	Х		Х	х	Х	Х

Mathematics is, like literature and art, part of our cultural heritage

History/Archeology	X	х		Х			X	x	
Journalism	X	X					X	x	
Languages/Linguistics	X	X		Х			X	x	
Law		X					X	x	
Materials Science/Nanotechnology	X	X	X	х		x	x	x	х
Mechanical engineering, Robotics	X	X	X	Х		х	X	x	х
Medicine/Pharmacy/Veterinary		х					X	x	
Music	X						X	x	
Painting						X	X		
Philosophy		х			X		X	х	
Physics	x	x	X	x	x	x	x	x	х
Poetry/Prose							X		
Psychology/Sociology/Anthropology	X	х		х			X	X	
Sculpture						X	X		х
Sewing/Knitting/Tapestry						x	X		х
Spirituality/Religions							X		
Theater/Acting							© Center for	Curriculum	Redesign

How much further away from Earth is the Sun than the Moon?



How much further away from Earth is the Sun than the Moon?

=



How much further away from Earth is the Sun than the Moon?

=





Prepare students to be ready to deal also with non-routine tasks

Strategic thinking

Prepare students to recognize and deal with lies

Mathematical reasoning and argumentation

Polish national curriculum (2008)



Matura 2014

Poziom podstawowy

Zadanie 31. (2 pkt)

Środek S okręgu opisanego na trójkącie równoramiennym ABC, o ramionach AC i BC, leży wewnątrz tego trójkąta (zobacz rysunek).





Zadanie 6. (3 pkt)

Trójkąt *ABC* jest wpisany w okrąg o środku *S*. Kąty wewnętrzne *CAB*, *ABC* i *BCA* tego trójkąta są równe, odpowiednio, α , 2α i 4α . Wykaż, że trójkąt *ABC* jest rozwartokątny, i udowodnij, że miary wypukłych kątów środko vych *ASB*, *ASC* i *BSC* tworzą w podanej kolejności ciąg arytmetyczny.



Egzamin gimnazjalny 2014

Zadanie 23. (0-3)

Z sześcianu zbudowanego z 64 małych sześcianów o krawędzi 1 cm usunięto z każdego narożnika po jednym małym sześcianie (patrz rysunek). Oblicz pole powierzchni powstałej bryły i porównaj je z polem powierzchni dużego sześcianu. Zapisz obliczenia.



Internet: I calculated like crazy, while it was enough to think!

PISA – levels of math competences



PISA – levels of math competences



Students at level 1 or below in EU (math)



Students at levels 5 or 6 in EU (math)



Mathematical reasononing – the weakest point in 2003



How to teach mathematical reasoning?



How to teach mathematical reasoning?

	5	8	*			6	2	
			9		7			
7	1			2			4	9
		3	2		5	8		
6								1
		9	6		4	5		
3	6			9			5	4
			4		1			
	8	4				9	1	

Explain why you can start solving this Sudoku by writing 1 in position *.



How to teach mathematical reasoning?





What is, roughly, the volume of a dollar bill?

Mathematical reasoning versus problem solving



OECD PISA test 2021 main domain: mathematics

How the above winds of change should influence this test?

1 Conference + 2 Colloquia with OECD





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Joan Ferrini-Mundy

Takura Baba



Zbigniew Marciniak

Jenni Ingram



Bill Schmidt

Julián Mariño

Core Experts Mathematics Expert Group (MEG)















Mathematical literacy is an individual's capacity to **reason mathematically** and to **formulate**, **employ, and interpret mathematics** to solve problems in a variety of real-world contexts.

It includes concepts, procedures, facts and tools to describe, explain and predict phenomena. It assists individuals to know the role that mathematics plays in the world and to make the well-founded judgments and decisions needed by constructive, engaged and reflective 21st century citizens.

More distant future?

More distant future?

Summary

Mathematics is much more than a toolbox.

Concept oriented teaching does not fit the present challenges. Teach the method of mathematics.

As it has always been, mathematics will then be the best answer to problems we face today.

It is so, because mathematics is one of the best parts of the cultural heritage of humanity.

Thank you!